Mesoscopic Josephson Effect

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In the classical Josephson effect the phase difference across the junction is well defined, and the supercurrent is reduced only weakly by phase diffusion. For mesoscopic junctions with small capacitance the phase undergoes large quantum fluctuations, and the current is also decreased by Coulomb blockade effects. We discuss the behavior of the current-voltage characteristics in a large range of parameters comprising the phase diffusion regime with coherent Josephson current as well as the supercurrent peak due to incoherent Cooper pair tunneling in the Coulomb blockade regime.

1. Introduction

The Josephson effect beautifully embodies quantum tunneling and superconductivity [1, 2]. Josephson systems have been a subject of fundamental research for decades, which have led to useful applications, e.g., in highly sensitive magnetometry and metrology. Like in the Ginzburg-Landau theory for bulk superconductivity, where the phase of the order parameter is considered as a quasiclassical variable, the phase difference across a Josephson junctions can frequently be treated classically. However, in the last ten years or so, new lithography and low-temperature techniques have allowed the fabrication and measurement of small Josephson junctions affected by the capacitive charging energy of single Cooper pairs [3, 4]. A large charging energy will render the Cooper pair number on either side of the junction classical and thus cause large quantum fluctuations of the conjugate phase variable.

In this article we show how the classical Josephson effect, that is a supercurrent I flowing at vanishing voltage V, gradually evolves via the classical phase diffusion regime into the supercurrent peak in the Coulomb blockade regime where Cooper pairs tunnel incoherently across the Josephson junction. After a brief review of the classical Josephson effect in sec. 2 and phase diffusion in sec. 3

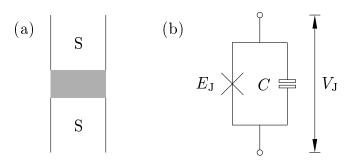


Fig. 1. (a) Schematic view of a Josephson junction where two superconductors are separated by an insulating barrier. (b) Equivalent circuit with Josephson coupling $E_{\rm J}$ and capacitance C. The voltage across the junction is denoted by $V_{\rm J}$.

we discuss Cooper pair tunneling in the Coulomb blockade regime in sec. 4. The turnover between the classical and the quantum regimes is discussed in sec. 5. Finally, sec. 6 contains some concluding remarks.

2. Classical Josephson Effect

A Josephson junction consists of two superconductors separated by a thin insulating barrier as shown in fig. 1a. Its dynamics may be described in terms of the phase difference φ of the two condensate wave functions on the left and right sides of the junction and the number n of Cooper pairs on the capacitor formed by the junction. These operators n and φ obey the commutation relation $[n, \varphi] = -\mathbf{i}$, and the junction Hamiltonian may be expressed as

$$H_{\rm J} = E_{\rm c} n^2 - E_{\rm J} \cos(\varphi). \tag{1}$$

The first term describes the charging energy associated with the capacitance C of the tunnel junction where $E_c = 2e^2/C$ is the charging energy corresponding to a single Cooper pair. The second term arises from the tunneling of Cooper pairs through the junction characterized by the Josephson coupling energy E_J . These properties may be expressed in terms of the circuit shown in fig. 1b.

The Josephson relations link the phase to the voltage across the junction

$$V_{\rm J} = \frac{\hbar}{2e} \dot{\varphi} \tag{2}$$

and to the supercurrent

$$I = I_{c} \sin(\varphi). \tag{3}$$

The critical current I_c is related to the Josephson coupling energy by $I_c = 2eE_J/\hbar$. These relations allow for a supercurrent flowing at zero voltage if φ remains constant in time.

3. Phase Diffusion in Josephson Junctions

In the real world Josephson junctions are coupled to an electromagnetic environment which may be described by an impedance $Z(\omega)$. For simplicity, we will in the following mostly consider the case

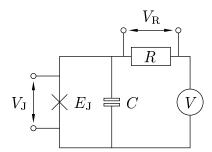


Fig. 2. Circuit modelling a real experimental set-up: a Josephson junction characterized by the Josephson energy $E_{\rm J}$ and capacitance C is coupled to a voltage source V via a resistor R. The voltage drops across the junction and the resistor are $V_{\rm J}$ and $V_{\rm R}$, respectively.

of an ohmic resistor $[Z(\omega) = R]$ but a more general case will be addressed in sec. 4. The resistor will give rise to Nyquist noise and therefore to a diffusive behavior of the phase difference φ .

To be specific, we consider the circuit shown in fig. 2 where the Josephson junction is coupled to the voltage source via an ohmic resistor. The voltages across the junction and the resistor are denoted be $V_{\rm J}$ and $V_{\rm R}$, respectively. It is useful to introduce the dimensionless resistance $\rho = R/R_{\rm Q}$ where $R_{\rm Q} = h/4e^2$ is the resistance quantum for Cooper pairs.

In the classical limit this system can be described by the Langevin equation [1, 5]

$$C\left(\frac{\hbar\ddot{\varphi}}{2e}\right) + \frac{1}{R}\left(\frac{\hbar\dot{\varphi}}{2e}\right) + I_{c}\sin(\varphi) = \frac{V_{R}}{R}.$$
 (4)

The term on the righthandside represents the Nyquist noise with $\langle \delta V_{\rm R}(t+\tau) \delta V_{\rm R}(t) \rangle = (2R/\beta)\delta(\tau)$ for a resistor at inverse temperature $\beta = 1/k_{\rm B}T$. Here, $\delta V_{\rm R}$ denotes the fluctuation of the voltage about its average value.

This problem has been solved by Ivanchenko and Zil'berman [6] in the overdamped limit where $2\pi^2\rho^2 E_{\rm J} \ll E_{\rm c}$. The stationary solution of the Fokker-Planck equation corresponding to eq. (4) can be expressed in terms of modified Bessel functions of complex order and yields the Cooper pair current [6]

$$\frac{I}{I_{\rm c}} = \operatorname{Im}\left(\frac{I_{1-\mathrm{i}\beta E_{\rm J}v}(\beta E_{\rm J})}{I_{-\mathrm{i}\beta E_{\rm J}v}(\beta E_{\rm J})}\right). \tag{5}$$

as a function of the dimensionless applied voltage $v = V/RI_{\rm c}$. While the supercurrent at zero voltage is destroyed by the fluctuations causing the phase diffusion, the current-voltage characteristics (5) display peaks at small but finite voltages as shown in fig. 3a. With decreasing temperature the I-V-curve (5) becomes closer to an ohmic line for voltages up to $RI_{\rm c}$, while the peak in the $I-V_{\rm J}$ -curve in fig. 3b moves towards zero voltage.

We analyze the result (5) by considering the zero bias differential resistance

$$R_0 = \left. \frac{\partial V_{\rm J}}{\partial I} \right|_{V_{\rm J}=0} = \left. \frac{\partial V}{\partial I} \right|_{V=0} - R. \tag{6}$$

 R_0 is defined with respect to the junction voltage $V_{\rm J}$, and $1/R_0$ describes the slope at the origin in fig. 3b. From eq. (5) one obtains

$$\frac{R_0}{R} = \frac{1}{I_0^2(\beta E_{\rm J}) - 1}. (7)$$

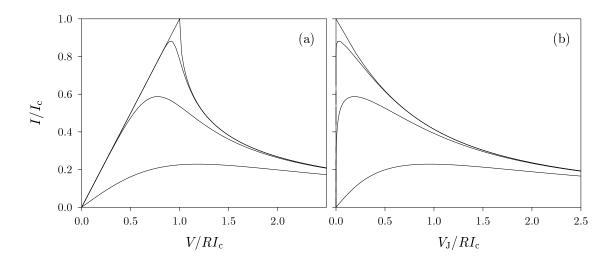


Fig. 3. (a) Cooper pair current-voltage characteristics I(V) [eq. (5)] in the overdamped phase diffusion regime for $\beta E_{\rm J} = 1, 5, 50$, and ∞ from the lower to the upper curve and (b) corresponding characteristics $I(V_{\rm J})$.

For $\beta E_{\rm J} \gg 1$, the I-V-curve is very close to I=V/R with an exponentially small difference

$$\frac{R_0}{R} = 2\pi\beta E_{\rm J} \exp(-2\beta E_{\rm J}). \tag{8}$$

This shows that for temperatures much lower than the height of the periodic potential for φ in eq. (1), the dynamics of the phase is thermally activated.

On the other hand, for $\beta E_{\rm J} \ll 1$ one finds in the overdamped limit

$$\frac{R_0}{R} = \frac{2}{(\beta E_{\rm J})^2}.\tag{9}$$

In this case, the I-V-curve becomes

$$I = \frac{I_{\rm c}^2}{2} \frac{RV}{V^2 + (2eR/\hbar\beta)^2} \tag{10}$$

which corresponds to a broad peak structure.

4. Coulomb Blockade in Josephson Junctions

We now turn to the case of ultrasmall tunnel junctions with spatial dimensions so small that $E_c \gg E_J$. Then the phase can no longer be treated as a quasiclassical variable, rather the charge on the junction capacitance will approximately follow classical statistics. As we have seen above, due to phase fluctuations, a supercurrent at zero voltage is no longer possible. However, a Cooper pair current may flow at finite voltages if the electromagnetic environment is able to absorb the energy 2eV gained by a Cooper pair tunneling through the junction. In contrast to sec. 3, it is now necessary the introduce the external impedance on the quantum level. Due to its linearity the external impedance may be modeled by a possibly infinite number of LC-oscillators. The corresponding

Hamiltonian then reads

$$H_{\rm imp} = \sum_{n=1}^{\infty} \left[\frac{q_n^2}{2C_n} + \left(\frac{\hbar}{2e}\right)^2 \frac{1}{2L_n} (\varphi_{\rm R} - \varphi_n)^2 \right]. \tag{11}$$

The external impedance in terms of the inductances L_n and capacitances C_n is given by

$$Z(\omega) = \left[\int_0^\infty dt e^{-i\omega t} \sum_{n=1}^\infty \frac{\cos(\omega_n t)}{L_n} \right]^{-1}$$
 (12)

where $\omega_n = (L_n C_n)^{-1/2}$. The coupling between the external impedance and the phase difference φ appears through the phase

$$\varphi_{R} = \frac{2e}{\hbar} \int_{0}^{t} dt' (V - V_{J}) = \frac{2e}{\hbar} V t - \varphi.$$
 (13)

This phase may formally be attributed to the resistance by making use of the Josephson relation (2).

Calculating the Cooper pair current from the Hamiltonian

$$H = H_{\rm J} + H_{\rm imp} \tag{14}$$

perturbatively to lowest order in $E_{\rm J}$, one obtains [7, 8]

$$I = \frac{\pi e E_{\rm J}^2}{\hbar} \left[P(2eV) - P(-2eV) \right]. \tag{15}$$

Here, P(2eV) and P(-2eV) are the probabilities that the energy 2eV of the tunneling Cooper pair is absorbed or provided by the environment, respectively. This probability depends on the external impedance and on temperature through [9]

$$P(E) = \frac{1}{2\pi\hbar} \int_{-\infty}^{+\infty} dt \exp\left[J(t) + \frac{i}{\hbar}Et\right]$$
 (16)

with

$$J(t) = 2 \int_{-\infty}^{\infty} \frac{d\omega}{\omega} \frac{\text{Re} Z_{t}(\omega)}{R_{Q}} \frac{e^{-i\omega t} - 1}{1 - e^{-\beta\hbar\omega}}.$$
 (17)

This expression contains the total impedance seen by the Josephson junction

$$Z_{t}(\omega) = \frac{1}{i\omega C + Z^{-1}(\omega)} \tag{18}$$

which is given by the external impedance in parallel with the capacitance.

For an ohmic environment $[Z(\omega) = R = \rho R_{\rm Q}]$ the result (15) may be evaluated further. At zero temperature one finds a zero bias anomaly given by $I \sim V^{2\rho-1}$. This shows that at T=0 the perturbative result (15) is only valid for large $\rho > 1/2$ where the current remains small for all voltages. In this case the I-V-curve displays a peak near voltages of order e/C as shown in fig. 4. This can easily be understood from a simple Coulomb blockade picture. At V=e/C the voltage gain 2eV just equals the charging energy E_c .

However, the experimentally relevant situation is an environment of low impedance ($\rho \ll 1$) [10]. On the one hand, it is difficult to fabricate large resistances at frequencies around E_c/\hbar , which typically is of the order of 10GHz, and on the other hand the resistance should not be too large to avoid heating. Furthermore, since charging effects are washed out by thermal fluctuations, we are interested in the regime of low but finite temperatures $\beta E_c \gg 1$. To proceed for parameters in

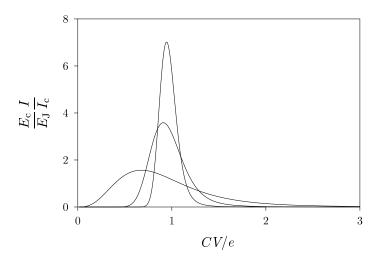


Fig. 4. Cooper pair current-voltage characteristics I(V) in the Coulomb blockade regime at zero temperature. The peak is sharpening with increasing $\rho = 2, 20, 100$.

this range, we first note that the function J(t) is equivalent to the position autocorrelation function of a free damped particle and can be evaluated in closed form for ohmic damping [11]. For long times, J(t) describes diffusive behavior linear in time for finite temperatures and logarithmic in time at zero temperature. We therefore neglect exponentially decaying terms. This restricts us to low voltages which is the regime of interest. Assuming furthermore $\rho \ll \beta E_{\rm c}$ in accordance with the above considerations, we arrive at [12]

$$J(t) = -2\rho \left(\ln \left[\frac{\beta E_c}{\pi^2 \rho} \sinh \left(\frac{\pi t}{\hbar \beta} \right) \right] + \gamma + i \frac{\pi}{2} sign(t) \right)$$
 (19)

Here, $\gamma = 0.5772...$ is the Euler constant. Inserting (19) into (16) and making use of (15) one finally obtains [12, 13, 14]

$$I = \frac{\pi}{2} I_c \frac{E_J}{E_c} \rho^{2\rho} \left(\frac{\beta E_c}{2\pi^2} \right)^{1-2\rho} \exp[-2\gamma \rho] \frac{|\Gamma(\rho - i\frac{\beta eV}{\pi})|^2}{\Gamma(2\rho)} \sinh(\beta eV). \tag{20}$$

This perturbative result is only correct if the current is not too large which may be the case for very small temperatures and very small damping. In fact, as noted above, at zero temperature one finds a divergence at low voltages. Therefore, the validity is restricted to not too low temperatures $\beta E_{\rm J} \ll \rho$. Since $E_{\rm c} \gg E_{\rm J}$, this together with the upper bound on temperature $[\beta E_{\rm c} \gg \rho]$ still leaves a rather large range where (20) is applicable.

The current-voltage characteristics (20) is shown in fig. 6 (see sec. 5) as dashed line for $\beta E_{\rm J} = 2$, $\rho = 0.04$ and $\beta E_{\rm c} = 1$ and 10^5 . It exhibits a peak at finite voltage which for small ρ is given by

$$V_{\text{max}} = \frac{\pi \rho}{e\beta} (1 + 4\zeta(3)\rho^3 + \ldots). \tag{21}$$

Here $\zeta(3) = 1.202...$ is a Riemann number. In the limit of small ρ , high temperatures and for $\beta eV \ll 1$ one recovers the result of classical phase diffusion (10).

A nonohmic environment of practical interest is a finite LC transmission line terminated by an

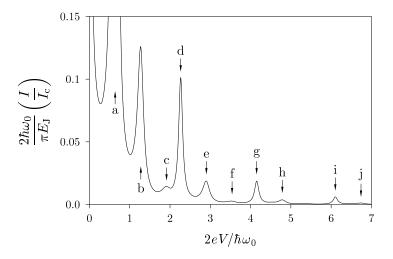


Fig. 5. Cooper pair current-voltage characteristic for an ultrasmall tunnel junction coupled to a finite transmission line with $R_{\rm L}/R_{\rm Q}=0.01, R_{\rm L}/R_{\infty}=0.1$, and $\omega_0 R_{\infty}C=1$ at zero temperature. The peaks correspond to excitations denoted by $(N_1N_2N_3N_4)$, where N_k is the number of quanta of the k-th mode excited. a: (1000), b: (2000), c: (3000), d: (0100), e: (1100), f: (2100), g: (0010), h: (1010), i: (0001), j: (1001).

ohmic load resistance R_L [15, 16]. The transmission line is characterized by its resistance at infinite length $R_{\infty} = (L_0/C_0)^{1/2}$ where L_0 and C_0 are specific inductance and capacitance per unit length. As a parameter describing the finite length ℓ of the transmission line we choose the $\lambda/4$ -frequency $\omega_0 = (\pi/2)u/\ell$ where $u = (L_0C_0)^{-1/2}$ is the velocity of wave propagation on the line.

Depending on the ratio between load resistance and resistance of the infinite transmission line, the environment behaves quite differently. For $R_L = R_{\infty}$ the impedance matching results in an ohmic impedance. On the other hand, for R_L very different from R_{∞} , the impedance displays sharp resonances. According to the above discussion, the properties of the external impedance should show up in the probability to absorb or emit energy, i.e. in P(E), and therefore according to (15) in the Cooper pair current-voltage characteristics. This is indeed the case as can be seen from fig. 5. There we show the zero temperature Cooper pair current for $R_L/R_{\infty} = 0.1$ obtained from a direct numerical evaluation of eqs. (15)–(17). The resonance peaks can be identified as single or multiple excitations of various transmission line modes [12]. The measurement of the Cooper pair current thus allows for a spectroscopy of the environmental modes.

5. Supercurrent Peak: Between the Phase Diffusion and Coulomb Blockade Regimes

So far, we have discussed the behavior of a Josephson junction in the classical overdamped limit (sec. 3) and in the quantum regime for charging energies much larger than the Josephson coupling energy (sec. 4). We now want to bridge the gap between these two limits by extending the perturbation theory presented in the previous section to infinite order in $E_{\rm J}$.

The summation of the perturbation series in $E_{\rm J}$ is only possible for an appropriate choice of the parameter regime. Motivated by the above discussion, we will continue to consider the overdamped regime where $\omega_R = 1/RC$ is much larger than the Josephson frequency $\omega_{\rm J} = (2e/\hbar)RI_{\rm c}$. This is

identical to the condition $2\pi^2\rho^2 E_{\rm J} \ll E_{\rm c}$ given in sec. 3. In addition, the correlation function J(t) contains a thermal frequency scale given by $\nu = 2\pi/\hbar\beta$ as can be seen from the last denominator in eq. (17). In the following we assume that $\omega_{\rm J} \ll \nu$ so that we may neglect terms exponentially decaying in time with ν or faster. This results in the approximation

$$J(t) = -2\rho \left[\frac{\pi}{\hbar \beta} |t| + S + i \frac{\pi}{2} sign(t) \right]$$
 (22)

valid for sufficiently high temperatures where $\rho \beta E_{\rm J} \ll 1$. Further, we have introduced the abbreviation

$$S = \gamma + \frac{\pi^2 \rho}{\beta E_c} + \psi \left(\frac{\beta E_c}{2\pi^2 \rho} \right)$$
 (23)

where $\psi(x)$ denotes the logarithmic derivative of the gamma function.

For the correlation function (22) the Cooper pair current can be evaluated exactly and expressed in terms of a continued fraction [17]

$$I = I_{c} \operatorname{Re} \left[\frac{\sin(\pi \rho)}{2\pi \rho} \frac{\exp(-2\rho S)}{v + i/\beta E_{J}} \frac{1}{1 + \frac{b_{1}}{1 + \frac{b_{2}}{1 + \dots}}} \right]$$
(24)

with coefficients

$$b_n = \left(\frac{\beta E_{\mathrm{J}}}{2\pi\rho}\right)^2 \frac{\sin(\pi\rho n)\sin(\pi\rho(n+1))\exp(-2\rho S)}{n(n+1)(n-\mathrm{i}v\beta E_{\mathrm{J}})(n+1-\mathrm{i}v\beta E_{\mathrm{J}})}.$$
 (25)

Since the continued fraction converges rapidly, we may linearize the sine functions appearing in eq. (25) for sufficiently small ρ . Then, the continued fraction may be evaluated with the help of a matrix recursion and one finds [17]

$$I = \frac{2e}{\hbar} E_{J}^{*} \operatorname{Im} \left(\frac{I_{1-i\beta eV/\pi\rho}(\beta E_{J}^{*})}{I_{-i\beta eV/\pi\rho}(\beta E_{J}^{*})} \right). \tag{26}$$

with an effective Josephson energy

$$E_{\mathrm{I}}^* = E_{\mathrm{I}} \exp(-\rho [\psi(1 + \hbar\beta\omega_{\mathrm{R}}/2\pi) + \gamma]). \tag{27}$$

Here we have rewritten the quantity S defined in eq. (23) in terms of the frequency ω_R and have neglected a term $\pi \rho/\hbar \beta \omega_R \ll 1$ in the overdamped limit considered. Even though ρ has to be small for the expression (27) to hold, the correction to the bare Josephson energy may be substantial because for low temperatures the ψ function grows logarithmically and may become large. On the other hand, in the classical limit where $\hbar \to 0$ and $e \to 0$ such that the flux quantum $\hbar/2e$ remains constant, the effective Josephson energy E_J^* coincides with the bare Josephson energy E_J . We thus recover in the classical overdamped limit the result (5).

In fig. 6 we show how the result (26) bridges between the phase diffusion result (5) shown as dotted line and the Coulomb blockade result (20) depicted as dashed line. The current-voltage characteristics have been calculated for $\beta E_{\rm J}=2$ and $\rho=0.04$. For large $\beta E_{\rm c}$ where charging effects should be important one obtains very good agreement with the Coulomb blockade result. With decreasing $\beta E_{\rm c}$ the current-voltage characteristics evolve differently and a crossover to the Ivanchenko-Zil'berman result is found.

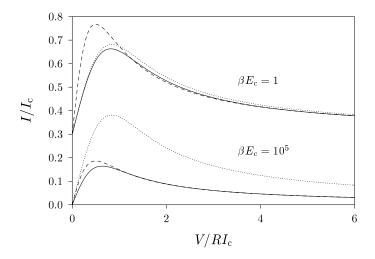


Fig. 6. The current-voltage characteristic of a Josephson junction with Josephson energy $\beta E_{\rm J}=2$ is shown for charging energies $\beta E_{\rm c}=1$ and 10^5 and external resistance $\rho=0.04$. The full line corresponds to our result (24) while the dotted line gives the standard Ivanchenko-Zil'berman (5) result and the dashed line depicts the prediction (20) for Coulomb blockade. The two sets of current-voltage characteristics are vertically shifted with respect to each other by $I/I_{\rm c}=0.3$ for sake of clarity.

6. Conclusions

We have studied the current-voltage characteristics of mesoscopic Josephson junctions focusing on the modifications of the supercurrent as the junction parameters change. We have not discussed here the effect of the charging energy on quasiparticle tunneling relevant at higher applied voltages only [18]. As the charging energy E_c grows relative to the Josephson energy E_J , the supercurrent of the classical Josephson effect was shown to evolve gradually into a supercurrent peak caused by incoherent Cooper pair tunneling. In the Coulomb blockade regime two types of structures may appear for small junctions with $E_J \ll E_c$ embedded in a standard low impedance environment. The first structure, a peak at low voltages has recently been seen in experiments on lithographically fabricated junctions [15, 16] as well as break junctions [19]. The second structure, peaks in the current-voltage characteristics due to resonances in the environmental impedance have also been seen in experiments [15, 16] with a well-defined environment consisting of two transmission line segments allowing for a quantitative test of the theoretical predictions and good agreement was found. Although detailed experimental studies of the region between the phase diffusion and Coulomb blockade limits are absent, recent work [20] indicates quantum effects in qualitative accord with the predictions made.

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